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Tian's invariant of the Grassmann manifold. (English, French summaries)

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Tian's invariant is of special interest in the study of Kähler-Einstein metrics with positive first Chern class. In this paper, the author proves that it is equal to $\frac{1}{p+q}$ for the complex Grassmann manifold $G_{p,q}(\mathbb{C})$, which is the natural generalization of the classical result for complex projective spaces.

The structure of $G_{p,q}(\mathbb{C})$ plays a crucial role in the argument, and the author also makes use of an imbedding of $(\mathbb{P}^1(\mathbb{C}))^p$ in $G_{p,q}(\mathbb{C})$. During the process, a nice description of the Grassmann manifold and a concise summary of general results on Tian's invariant are included for the reader's convenience. *Zhou Zhang*

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Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.